

Antiderivatives

- To prove $F(x)$ is antiderivative of $f(x) \Rightarrow F'(x) = f(x)$.
- $\int f(x)dx = F(x) + C$
- $\int f'(x)dx = f(x) + C$
- $\int u^n du = \frac{u^{n+1}}{n+1} + C$
- $\int \frac{du}{u} = \ln|u| + C$
- $\int \frac{1}{ax+b} dx = \frac{1}{a} \ln|ax+b| + C$
- $\int e^{ax+b} dx = \frac{1}{a} e^{ax+b} + C$
- Integration by parts: $\int u dv = u \cdot v - \int v du$
- Area between (C_f) and (C_g) from $x = a$ to $x = b$: $A = \int_a^b |f(x) - g(x)| dx$
- Volume = $V = \int_a^b \pi (f(x))^2 dx$
- $\cos^2 x = \frac{1 + \cos 2x}{2}$
- $\sin^2 x = \frac{1 - \cos 2x}{2}$
- $\int \cos ax dx = \frac{1}{a} \sin ax + C$
- $\int \sin ax dx = -\frac{1}{a} \cos ax + C$



Let $f(x)$ and $g(x)$ be two continuous functions defined on $\mathbb{R}$.

A , B , and C are real constants.

n is a natural number.

$$\int A \cdot f(x) \cdot dx = A \cdot \int f(x) \cdot dx$$

$$\int [A \cdot f(x) \pm B \cdot g(x)] \cdot dx = \int A \cdot f(x) \cdot dx \pm \int B \cdot g(x) \cdot dx$$

$$\int (Ax + B)^n \cdot dx = \frac{(Ax + B)^{n+1}}{A \cdot (n + 1)} + C \quad (n \neq -1, A \neq 0)$$

$$\int_A^A f(x) \cdot dx = 0$$

$$\int_A^B f(x) \cdot dx = - \int_B^A f(x) \cdot dx$$

$$\int_A^B f(x) \cdot dx + \int_B^C f(x) \cdot dx = \int_A^C f(x) \cdot dx$$

